

# Promotion Dynamics Analysis of Photovoltaics Based on Feed-in Tariff



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## Today's Topic ( January 17th )

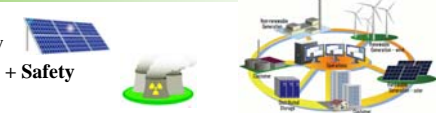
- Background and Objective
- Definition of Model
- Promotion Dynamics Analysis of PV  
( 1 decision player in a community )
- ( Promotion Dynamics Analysis of PV )  
( 2 decision player in a community )  
( Note : Next group meeting )
- Summary



## Introduction

### Energy Problem[1]

- Stable energy supply
  - Low emission
  - Energy secure
- + Safety



### New Resource of Energy

#### Photovoltaics : PV

##### Advantage

Self energy management



##### Disadvantage

High cost of PV panel

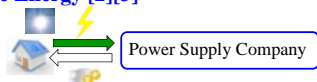


Output variability

### Promotion Policy of Renewable Energy [2][3]

#### Feed-in Tariff (FIT)

PV for residential setting



It is important to balance between promotion PV and consumer's load 3



## Objective

### Objective of Research

#### Promotion Dynamics Analysis of PV

- Robustness against imbalance of PV
- Energy Secure (Self energy management)



### Problems

- Complex connections between agents

⇒ Promotive rate of PV  
Evolutionary Game[4]

- Variance of output

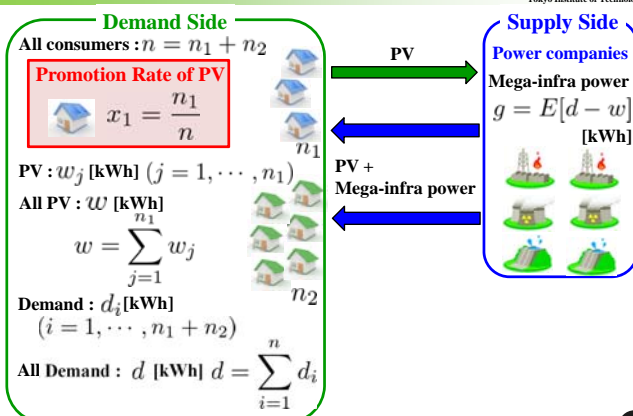
⇒ Risk function

- High cost of PV

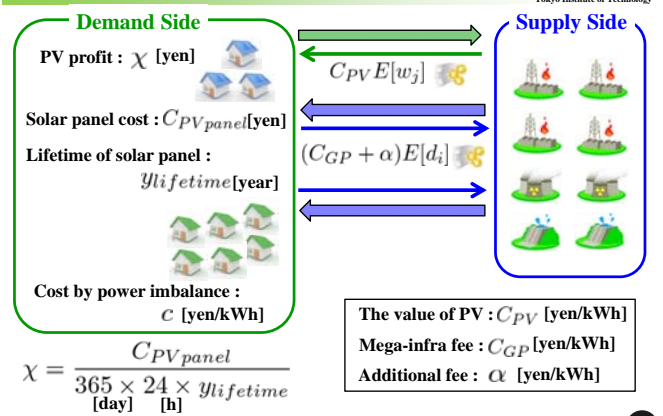
⇒ Reallocation for promotive PV



## Parameters Based on Feed-in Tariff



## Parameters Based on Feed-in Tariff



### Power Imbalance Risk

Power balance : Load Frequency Control (LFC) [5]

$$|d - (w + E[d - w])| \leq \epsilon E[d]$$

(Demand) - (Supply) Ability of power control

The value of  $\epsilon$  : 0.01 ~ 0.02 (1 ~ 2%) [5]

If  $|d - (w + E[d - w])| > \epsilon E[d]$ , then power imbalance occurs

**Assumption 1**

- $w_j$  and  $d_i$  are stochastic variables [6]
- $\{w_j\}_{j \in \mathcal{V}}$  and  $\{d_i\}_{i \in \mathcal{N}}$  are independent and identically distributed
- Each  $w_j$  and  $d_i$  are independent

**R: Probability of Power Imbalance**

$$R = \Pr\{|w - n_1 E[w_i]| > \epsilon n E[d_i]\} = \Pr\left\{\frac{|w - n_1 E[w]|}{\sqrt{n_1 \sigma}} > \frac{\epsilon n E[d_i]}{\sqrt{n_1 \sigma}}\right\}$$

$$\approx \frac{2}{\sqrt{2\pi}} \int_{\frac{\epsilon n E[d_i]}{\sqrt{n_1 \sigma}}}^{\infty} e^{-\frac{t^2}{2}} dt = \text{erfc}\left(\frac{\epsilon n E[d_i]}{\sqrt{2n_1 \sigma}}\right)$$

PV rate increase, then risk increase

### Process of New Imbalance Risk

It is too strong condition to assume independent of PV

All PV generate power at same time : -

Imbalance Risk existed between - and -

Small risk!

We define new risk function

$$\begin{cases} R_1(x_1) = -a(1-x_1)^2 + a \\ R_2(x_1) = ax_1 \\ R_3(x_1) = ax_1^2 \end{cases}$$

### Utility of PV Installer and No PV Installer

**Expectation Utility of PV Installer :  $y(x_1)$**

$$y(x_1) = -(1 - R(x_1))\{(C_{GP} + \alpha)E[d_i] + \chi - C_{PV}E[w_j]\} - R(x_1)cE[d_i]$$

**Expectation Utility of No PV Installer :  $z(x_1)$**

$$z(x_1) = -(1 - R(x_1))\{(C_{GP} + \alpha)E[d_i]\} - R(x_1)cE[d_i]$$

### Promotion Dynamics of PV

**Promotion Dynamics of PV (#)**

$$\dot{x}_1 = (f_1(x_1) - \phi(x_1))x_1$$

If PV installation is better than average strategy, PV installation increases

$f_1(x_1) = y(x_1)$  ( $f_1(x_1)$ : Expectation of selecting strategy 1)

$\phi(x_1) = y(x_1)x_1 + z(x_1)(1 - x_1)$  ( $\phi(x_1)$ : Average expectation)

Promotion rate of PV :  $x_1$       Expectation of PV installer :  $y(x_1)$

Expectation of no PV installer :  $z(x_1)$

### Promotion Dynamics of PV

**Promotion Dynamics of PV (#)**

$$\dot{x}_1 = (f_1(x_1) - \phi(x_1))x_1$$

$$f_1(x_1) = y(x_1)$$

$$\phi(x_1) = y(x_1)x_1 + z(x_1)(1 - x_1)$$

**Concrete Objective**

Theoretic analysis between Imbalance Risk and PV promotion rate on promotion dynamics of PV (#)

**Existence of stable points**

$$(f_1(x_1) - \phi(x_1))x_1 = 0, \quad \frac{d((f_1(x_1) - \phi(x_1))x_1)}{dx_1} < 0 \quad (*)$$

**Existence of unstable points**

$$(f_1(x_1) - \phi(x_1))x_1 = 0, \quad \frac{d((f_1(x_1) - \phi(x_1))x_1)}{dx_1} > 0 \quad (**)$$

### Simulation of Promotion Dynamics (#)

**Common Parameters Setting**

- All consumer  $n = 1,000,000$
- PV power [\*]  $E[w_j] = 0.4268$  [kWh]
- Demand [7]  $E[d_i] = 0.7336$  [kWh]
- PV fee [\*\*]  $C_{PV} = 42$  [yen/kWh]
- Mega-infra fee  $C_{GP} = 16$  [yen/kWh]
- Cost by power imbalance [8]  $c = 1,000$  [yen/kWh]
- Solar panel cost  $C_{PVpanel} = 2,000,000$  [yen]
- Lifetime of solar panel  $Y_{lifetime} = 10$  [year]

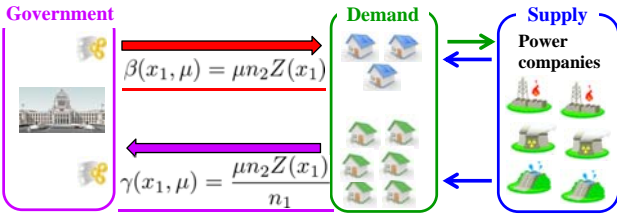
**Result (Note)**

Dynamics (#) convergence only  $x_1 = 0$  or  $x_1 = 1$  ( $\chi$  is the dominated member)

Next, We consider concrete reallocation  $\beta$  and  $\gamma$

## Reallocation Mechanism ( Model 1 )

### Model of promotion Dynamics of PV with reallocation ( Model 1 )



$$Z(x_1) = ((1 - R(x_1))C_2 + R(x_1)C_4)$$

$$C_4 = cE[d_i]$$

$$C_2 = C_{GP}E[d_i]$$

## Utility with Reallocation ( Model 1 )

Expectation Utility of PV Installer :  $y(x_1, \mu)$

$$y(x_1, \mu) = -(1 - R(x_1))\{(C_{GP} + \alpha)E[d_i] + C_1\} - R(x_1)C_4 + \frac{\mu n_2 Z(x_1)}{n_1}$$

The diagram shows a flow: Demand (blue box) points to Supply (blue box), which points to Government (purple box), which points to Demand (green box). There are question marks near the Supply and Government boxes.

$$C_1 = \chi - C_{PV}E[w_j]$$

Expectation Utility of No PV Installer :  $z(x_1, \mu)$

$$z(x_1, \mu) = -(1 - R(x_1))\{(C_{GP} + \alpha)E[d_i]\} - R(x_1)C_4 + \mu Z(x_1)$$



## A Theorem of Model 1

### Theorem 1

Suppose that risk function is  $R = R_1(x_1) = -a(x_1 - 1)^2 + a$ . Under the assumption of given  $x_1$ , the promotion dynamics of PV (##) has stable points iff the bellow condition of  $a$  is satisfied such that

$$0 < a < \frac{((2 + A)x_1 - 4) + \sqrt{(A^2 + 8A)x_1^2 - 24Ax_1 + 16A}}{2(A - 1)x_1(x_1 - 2)^2} \quad (1)$$

### Sketch of Proof

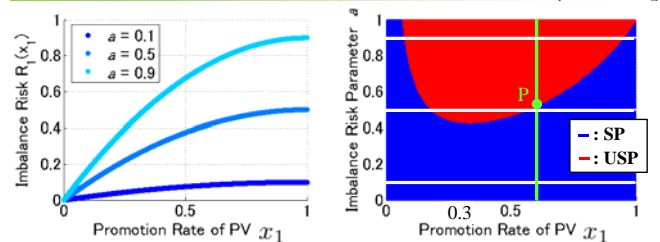
(##) can represent  $\dot{x}_1 = x_1(1 - x_1)(y(x_1, \mu) - z(x_1, \mu))$ . Calculating these inequalities (\*), we can lead the above condition.

The inequality (1) says there are no relation between stable points and  $C_{PV}$ . And we transform the inequality (1) and represent  $A = c/C_{GP}$ , then

$$0 < a < \frac{2}{x_1 \left( \sqrt{((2 + A)x_1 - 4)^2 + 4(A - 1)(x_1 - 2)^2} - ((2 + A)x_1 - 4) \right)}$$

The cost by power imbalance  $c$  prevents from promotion of PV

## Simulation of Model 1 ( $R=R_1$ )



On simulation with common parameters ( p. 10 ),

- If we want to promote PV about 30% [1] ( $x_1 = 0.6$ ) in  $R = R_1(x_1)$  a max of parameter  $a$  is under point P

## Summary ( January 17th )

### Summary

Promotion dynamics analysis of PV ( 1 decision player in a community )

- Formulation of Promotion dynamics of PV
- Derivation of the relation between a reachable PV rate and parameters
- Simulation



### Next ( Group meeting on January 21st )

2 decision players in a community

- Formulation of Promotion dynamics of PV
- The promotion dynamics Analysis by simulation

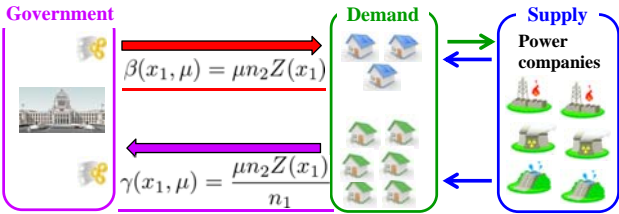


## Today's Topic ( January 21st )

- Background and Objective
- Definition of Model
- Promotion Dynamics Analysis of PV ( 1 decision player in a community ) ( Note : The contents of local group meeting )
- Promotion Dynamics Analysis of PV ( 2 decision player in a community )
- Progress

## Reallocation Mechanism ( Model 1 )

Model of promotion Dynamics of PV with reallocation ( Model 1 )



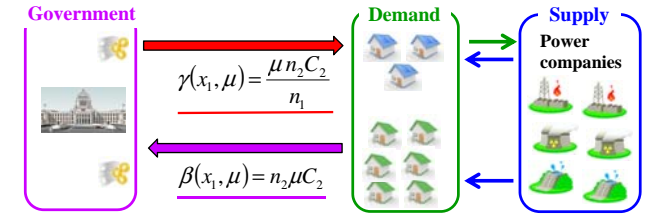
$$Z(x_1) = ((1 - R(x_1)C_2 + R(x_1)C_4)$$

$$C_4 = cE[d_i]$$

$$C_2 = C_{GP}E[d_i]$$

## Reallocation Mechanism ( Model 2 )

Reallocation from no PV installer to PV installer



$$C_1 = \chi - C_{PV}E[w_j]$$

Expectation Utility of PV Installer :  $y(x_1, \mu)$

$$y(x_1, \mu) = -(1 - R(x_1))\{(C_{GP} + \alpha)E[d_i] + C_1\} - R(x_1)C_4 + \frac{\mu n_2 C_2}{n_1}$$

Expectation Utility of No PV Installer :  $z(x_1, \mu)$

$$z(x_1, \mu) = -(1 - R(x_1))\{(C_{GP} + \alpha)E[d_i]\} - RC_4 - \mu C_2$$

## A Theorem of Model 2

**Theorem 4**  
Suppose that risk function is  $R = R_1(x_1) = -a(1 - x_1)^2 + a$ .  
Under the assumption of given  $x_1$ , the promotion dynamics of PV (##) has stable points iff the bellow condition of  $a$  is satisfied such that

$$0 < a < \frac{1}{x_1(4 - 3x_1)} \quad (4)$$

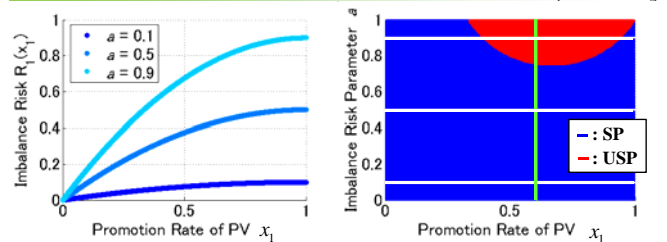
**Sketch of Proof**  
Same as sketch of proof about theorem 1.

The inequality (4) says there are no relation between stable points and parameters  $C_{PV}$ ,  $C_{GP}$ ,  $c$ , and so on.

The minimum upper bound of  $a$  is 0.75 when  $x_1$  equals 2/3.

$$\therefore \frac{1}{x_1(4 - 3x_1)} = \frac{1}{-3(x_1 - 2/3) + 4/3}$$

## Simulation of Model 2 ( R=R<sub>1</sub> )



On simulation with common parameters ( p. 10 ) supposed that  $R = R_1(x_1)$ ,  
• If we want to promote PV about 35% [ $x_1 = 0.6$ ] ( green line ),  
a parameter  $a$  is no constraint if  $a < 0.75$ .

Percentage of demand power =  $0.35 \times \frac{E[d_i]}{E[w_j]} = 0.35 \times \frac{0.7336}{0.4268} \approx 0.60$

## Mixture of Strategies

Motivation



**System**  
Mixture of 2 Learning Algorithms (LAs)  
LA1 : Replicator Dynamics (RD)  
LA2 : Imitation



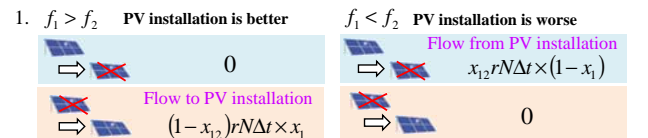
PV rate of LA1 :  $x_{11}$   
PV rate in LA2 :  $x_{12}$   
Rate of LA1 in a community :  $\eta$   
Imitation rate :  $r$

$$\text{PV rate of all consumers : } x_1 = \eta x_{11} + (1 - \eta)x_{12}$$

## Imitation[9]

**Decision Sequence**

- Select an agent and an opponent randomly
- If the opponent looks good, the agent imitates opponent's strategy



- Variance of the number of PV installation**  

$$\begin{cases} N\Delta x_{12} = x_1(1 - x_{12})rN\Delta t & (f_1 > f_2) \\ N\Delta x_{12} = -x_{12}(1 - x_1)rN\Delta t & (f_1 < f_2) \end{cases}$$

$$\dot{x}_1 = \begin{cases} rx_1(1 - x_{12}) & (f_1 \geq f_2) \\ 0 & (f_1 = f_2) \\ -rx_{12}(1 - x_1) & (f_1 < f_2) \end{cases}$$

**Imitation ( Most easily model )**



### Simulation Setting

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#### Promotion Dynamics of PV (mixture of LAs) (###)

$$x_1 = \eta x_{11} + (1-\eta)x_{12}$$

$$\text{LA1} : \dot{x}_{11} = x_{11}(1-x_1)(y(x_1, \mu) - z(x_1, \mu))$$

$$\text{LA2} : \dot{x}_{12} = \begin{cases} rx_1(1-x_{12}) & (y(x_1, \mu) > z(x_1, \mu)) \\ 0 & (y(x_1, \mu) = z(x_1, \mu)) \\ -rx_{12}(1-x_1) & (y(x_1, \mu) < z(x_1, \mu)) \end{cases}$$

Utility of PV installer :  $y(x_1, \mu)$  ← Same as p. 19

Utility of no PV installer :  $z(x_1, \mu)$



$x_{11}$  : PV rate of LA1  
 $x_{12}$  : PV rate in LA2  
 $\eta$  : Rate of LA1 in community  
 $r$  : Imitation rate

#### Concrete Objective

analysis between Imbalance Risk and PV popularization rate on promotion dynamics of PV (###) by simulation ( $x_1 = [x_{11} \ x_{12}]^T$ )

Existence of stable points

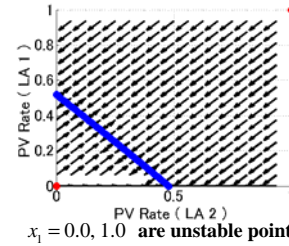
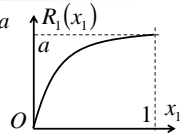
$$\dot{x}_1 = 0, \frac{dx_1}{dx_1} = \begin{bmatrix} \partial \dot{x}_{11} / \partial x_{11} & \partial \dot{x}_{11} / \partial x_{12} \\ \partial \dot{x}_{12} / \partial x_{11} & \partial \dot{x}_{12} / \partial x_{12} \end{bmatrix} < 0 \quad (***)$$



### Simulation of Promotive Dynamics (###)

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- Risk of Imbalance :  $R(x_1) = R_1(x_1) = -a(1-x_1)^2 + a$
- Imitation rate :  $r = 0.001$
- Rate of LA 1 agents :  $\eta = 0.5$
- Common parameters are same as p. 10
- Model 2 is used



$x_1 = 0.0, 1.0$  are unstable points

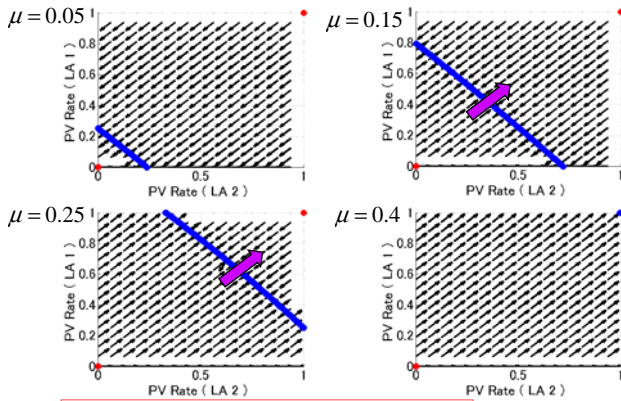
There are linear shaped stable points

- Stable point : ●
- Unstable point : ●
- Vector fields : →
- Learning Algorithm(LA)1
- Replicator Dynamics
- Learning Algorithm(LA)2
- Imitation
- Reallocation rate :  $\mu = 0.1$
- Risk fun. parameter :  $a = 0.1$



### Changes of Reallocation Rate

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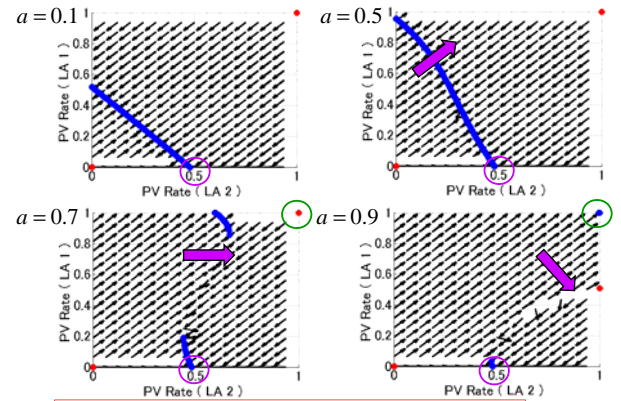


A parameter  $\mu$  relates the total PV rate  $x_1$



### Changes of Imbalance Risk Parameter

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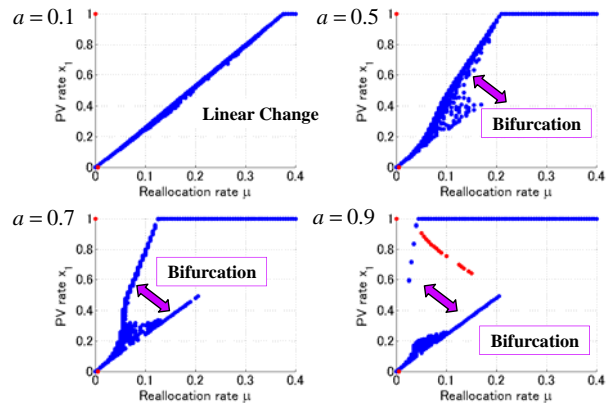


A parameter  $a$  relates the shape of stable points



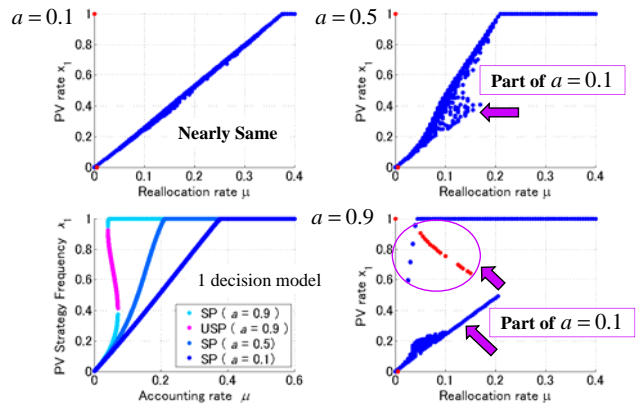
### Distribution of promotive rate of PV

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### Comparison of 1 Decision Model

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## Summary ( January 21st )

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### Summary

Promotion dynamics analysis of PV

- 1 decision player in a community
- Formulation of Promotion dynamics of PV
- Derivation of the relation between a reachable PV rate and parameters
- Simulation



- 2 decision players in a community
- Formulation of Promotion dynamics of PV
- The promotion dynamics Analysis by simulation



### Feature Works

- More than 3 strategy
- Derivation of parameter's relation about promotion dynamics with 2 decision players in a community



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## References

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- [1] 経済産業省, "エネルギー政策見直しの基本的視点," June, 2011.
- [2] Yamada, Ikki, "National Survey Report of PV Power Applications in Japan 2011," International Energy Agency Co-operative Programme on Photovoltaic Power Systems, May 31, 2012.
- [3] 岩屋, "ドイツ太陽光発電市場 現地調査報告," 経営センサー, November, 2010.
- [4] M. A. Nowak, "進化のダイナミクス : 生命の謎を解き明かす方程式," 共立出版, 2009.
- [5] 奥田, 木村, "太陽光発電システムの出力変動抑制技術," 東芝レビュー, Vol.65 No.9, 2010.
- [6] E. Y. Bitar, P. P. Khargonekar and K. Poolla, "Systems and Control Opportunities in the Integration of Renewable Energy into the Smart Grid," *18th International Federation of Automatic Control World Congress*, pp. 4927-4932, 2011.
- [7] 電気事業連合会, "2011年度分 電力需要実績(確報)," April 27th, 2012.
- [8] 今中, "需給対策コストカーブの外観," (財) 電力中央研究所社会経済研究所ディスカッションペーパー, 2011.
- [9] 大浦, "社会科学者のための進化ゲーム論 : 基礎から応用まで," 勁草書房, 2010.

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