

# Cooperative reaching control for bimanual robotic system

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## Outline

### Introduction

Present and past research  
Motivation

### Background

Control of Robot Manipulator

### Problem Setting

Bimanual robot manipulators  
Cooperative Reaching Controller

### Stability

Closed loop system  
Stability analysis

### Simulation

Simulation Setting  
Simulation Result

### Conclusion and future works

## Over view

### Cooperative control

Control multiple agents to achieve one common project

- Examples of cooperative control
  - Formation, Sensor networks, Coverage Problem ect.
  - Bimanual robot arm motion, Cooperative operation, Man-machine Cooperation ect.

Human may have the finest cooperative ability

### Cooperative on human being

- bimanual movement, walking ect.

Focus on the cooperative of human being!

## Present works

### Present works on robotics

- Arimoto et al. 2005 : Reaching for redundant manipulators
- Spong et al. 2006 : Output synchronization
- Nijmeijer et al. 2004 : Synchronization of robot manipulators
- Utiyama et al. 2000 : Space Telerobotics
- S. Amano et al. 2007 : Modeling of Dual-arm Robot

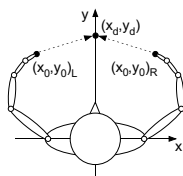
### Present works on physiology

- Corbetta et al. 2002 : Two-hand reaching of infants
- White et al. 1964 : synchronization of two hand reaching movement
- D. Nozaki 2007 : Analysis of unimanual and bimanual movements

## Motivation

### definition (Cooperative Reaching)

Use the cooperative control scheme to cooperate two manipulators reach a desired target point



### Motivation

Cooperate bimanual manipulators' reaching movement

## Motivation

### Where to use?

- Space robot : Dual arm operation robot
- Rehabilitation Robot



From "Kobe robot technology project",  
"http://www.kobe-rt.jp/index.shtml"

- Humanoid robot

## Manipulator dynamics

### The Euler-Lagrange equations

$$M(q)\ddot{q} + C(q, \dot{q})\dot{q} + g(q) = \tau$$

$$y = \dot{q} \tag{1}$$

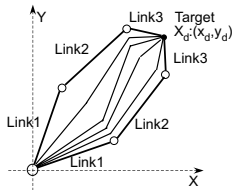
- $q, \dot{q}, \ddot{q} \in \mathbb{R}^n$ : Manipulator joint angular, velocity, accelerate
- $M \in \mathbb{R}^{n \times n}$ : Positive definite inertia matrix
- $C \in \mathbb{R}^{n \times n}$ : Centripetal and Coriolis torques
- $g \in \mathbb{R}^n$ : Gravitational torques
- $\tau \in \mathbb{R}^n$ : generalized forces acting on the system

### Redundant Manipulator

A manipulator has more articulate degrees of freedom than are required for a given object

## Control for redundant manipulators

- Self Motion  $\rightarrow$  manipulator joint states uncertain



- On redundant manipulator control, dimension difference between the joint states and end-point

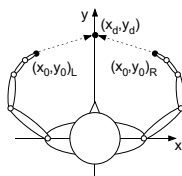


To control the redundant manipulator, have to solve previous problems

## Bimanual robot manipulators

- Dual-manipulator located as the same as the two arms of human

$$M_i \ddot{q}_i + C_i \dot{q}_i + g_i = \tau_i, i = L, R \tag{6}$$



Planar manipulator

$\rightarrow$  Ignore the gravitational torques  $g_i$

## Control of robot manipulators

- Motion control
  - Joint space coordinate based
  - Tracking the desired position and velocity  $q \rightarrow q_d, \dot{q} \rightarrow \dot{q}_d$
  - Controller :

$$\tau = M(q)\ddot{q}_d + C(q, \dot{q})\dot{q}_d + g(q) - K_d \dot{e} - K_p e$$

$$e = q - q_d, \dot{e} = \dot{q} - \dot{q}_d \tag{2}$$

$q_d, \dot{q}_d, \ddot{q}_d$  denote the desired joint angle, velocity, accelerate  
 $K_p, K_d$  : Positive defined control gain

- Reaching Control
  - Task space coordinate based
  - Reaching the target point in task space  $x \rightarrow x_d$
  - Controller :

$$\tau = g(q) - K_d \dot{\Delta}x - K_p J_x^T \Delta x$$

$$\Delta x = x - x_d \tag{3}$$

$x, x_d$  : current end-point position and desired end-point position  
 $J_x^T$  : Jacobian Matrix

## Reaching Control for redundant manipulators

- Arimoto reaching control for redundant manipulators
- Controller : The same as nonredundant manipulators

$$\tau = g(q) - K_d \dot{\Delta}x - K_p J_x^T \Delta x$$

$$\Delta x = x - x_d \tag{4}$$

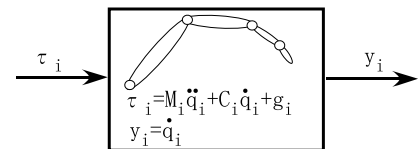
- Stability :  
 "Stability on an EP manifold", and "Transferability to an EP Manifold"  
 Energy Function :

$$W = \frac{1}{2} \dot{q}^T M(q) \dot{q} + \frac{1}{2} \Delta x^T K_p \Delta x + \alpha \sqrt{K_p} \Delta x^T (J^T)^T M \dot{q} \tag{5}$$

$\alpha$  : A very small positive define constant to make sure stability  
 $K_p, K_d$  : Positive defined control gain

## Bimanual robot manipulator

- For each manipulator  $i = L, R$



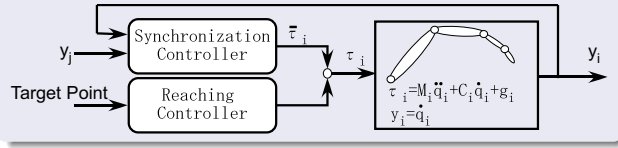
$\Rightarrow \tau_i$ : Input,  $\dot{q}_i$ : Output

### Passivity

- Kinetic energy as storage :  $V_i = \frac{1}{2} \dot{q}_i^T M_i \dot{q}_i$
- Passive from input  $\tau_i$  to output  $\dot{q}_i$  as  $\dot{V}_i = \tau_i^T \dot{q}_i - g_i$ 
  - Lossless for  $g_i = 0$
  - Strictly passive for  $g_i \neq 0$  :  $\dot{V}_i < \tau_i^T \dot{q}_i$

## Cooperative reaching control

### System Block Diagram



Cooperative reaching controller contains two parts

- Reaching Controller to reach target point

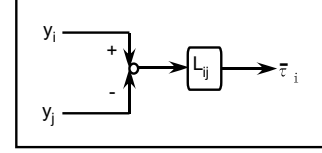
$$u_i = -K_{d,i}\dot{q}_i - J_{x_i}^T K_{p,i} \Delta x_i, i = L, R \quad (7)$$

- Target Reaching requires  $u_i = 0$  for  $\Delta x_i = 0 \Rightarrow x_i = x_d$
- Synchronization Controller requires information sharing to cooperate

## Interconnection for two manipulators

- Synchronization controller

Synchronization Controller



$\bar{\tau}_i, i = L, R$  : New input for synchronization

$y_i, y_j$  : Output of each manipulator

- Interconnection : Linear protocol

$$\bar{\tau}_i = L_{ij}(y_i - y_j) = \Delta \dot{q}_{ij}, i = L, R$$

$$\Delta \dot{q}_{ij} = \dot{q}_i - \dot{q}_j = y_i - y_j :$$

- Synchronization  $\Rightarrow \bar{\tau}_i = 0$  for  $y_L = y_R$

Cooperative Reaching Controller :  $\tau_i = \bar{\tau}_i + u_i$

## Closed loop system

### Closed loop system

$$M_i \ddot{q}_i + C_i \dot{q}_i + K_{d,i} \dot{q}_i + J_{x_i}^T K_{p,i} \Delta x_i = \bar{\tau}_i, i = L, R \quad (8)$$

### assumption

- control gain  $K_{p,L}, K_{p,R}, K_{d,L}, K_{d,R}$  : positive definite
- coupling gain  $\lambda_{LR}, \lambda_{RL}$  : semi-positive define &  $K_{d,L} \lambda_{LR} = K_{d,R} \lambda_{RL}$
- Jacobian Matrix  $J_x$  : non-singular

### The Goal

Asymptotic to reaching the target point :  $x_i = x_d, i = L, R$

Joint velocity symmetric synchronization :  $\dot{q}_L = -\dot{q}_R$

(Want joint position symmetric synchronization :  $q_L = -q_R$ )

## Stability for non-redundant manipulators

### Theorem

For previous assumption, equilibrium states  $(q_d, 0)$  corresponding to the target position  $x_d$  in closed-loop system (8) are asymptotically stable in a local sense

### Proof.

- Storage Function :

$$V_i = \frac{1}{2} \dot{q}_i^T M_i \dot{q}_i + \frac{1}{2} \Delta x_i^T K_{p,i} \Delta x_i$$

$$\dot{V}_i = -\dot{q}_i^T K_{p,i} \dot{q}_i - \dot{q}_i^T K_{d,i} \lambda_{ij} \Delta \dot{q}_{ij}, i = L, R$$

- Overall system storage :

$$V = V_L + V_R$$

$$\frac{d}{dt} V = -\dot{q}_L^T K_{p,L} \dot{q}_L - \dot{q}_R^T K_{p,R} \dot{q}_R - \Delta \dot{q}_{LR}^T K_{d,R} \lambda_{RL} \Delta \dot{q}_{LR} \leq 0$$

- $\dot{V} = 0 \iff \dot{q}_L = -\dot{q}_R = 0$

$\Rightarrow$  Asymptotically Stable □

## Stability for redundant manipulators

### Problem of the redundant manipulators case

Storage function V can't be positive definite for the self-motion

- First Step: Ignore self-motion to stabilize reaching control  
The same as non-redundant case

$$\Rightarrow V_i = \frac{1}{2} \dot{q}_i^T M_i \dot{q}_i + \frac{1}{2} \Delta x_i^T K_{p,i} \Delta x_i$$

- Consider a additional energy function to stabilize self-motion for each manipulator  $\alpha \sqrt{K_{p,i}} \Delta x_i^T (J^\dagger)^T M_i \dot{q}_i$

$\Rightarrow$  overall system storage function as :

$$W_i = V_i + \alpha \sqrt{K_{p,i}} \Delta x_i^T (J^\dagger)^T M_i \dot{q}_i, i = L, R$$

$$\Rightarrow W = W_L + W_R \quad (9)$$

Where  $\alpha$  is a positive constant.

- Use next inequation

$$\alpha \sqrt{K_p} \Delta x^T (J^\dagger)^T M \dot{q} \leq \frac{\alpha}{2} K_p \Delta x^T (J^\dagger)^T M J^\dagger \Delta x + \frac{\alpha}{2} \dot{q}^T M \dot{q} \quad (10)$$

$$W_i \geq \frac{1-\alpha}{2} \dot{q}_i^T M_i \dot{q}_i + \frac{K_{p,i}}{2} (1-\alpha h_{0i}) \|\Delta x_i\|^2 = W_{im}, i = L, R \quad (11)$$

where,  $\lambda_M \{(J^\dagger)^T M_i J^\dagger\} \leq h_{0i}$

- if the positive  $\alpha$  is small enough,  
 $W_i \geq W_{im} \geq 0 \Rightarrow W \geq W_{Lm} + W_{Rm} = W_m \geq 0$
- for a given  $\alpha \geq 0$  there exists a  $\gamma(\alpha)$  such that

$$\frac{dW}{dt} \leq -\gamma(\alpha) W \leq -\gamma(\alpha) W \quad (12)$$

- which means  $W_m(t) \leq W(t) \leq e^{-\gamma(\alpha)t} W(0)$

$\Rightarrow$  Exponentially stability

### Advantage and disadvantage of this method

#### Advantage

- Simple reaching controller
- Don't need calculate the pseudo-inverse Jacobian matrix

#### Disadvantage

- Cannot use to obstacle and singularity avoidance
- Synchronization on the velocity level  $\Rightarrow$  Cannot satisfy the position synchronization

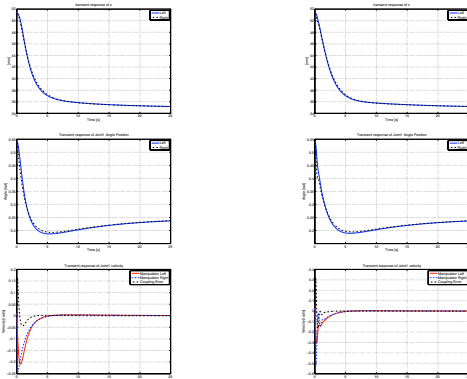


- Synchronize information  $\dot{q} \rightarrow q$  and  $\dot{q}$
- Take the output as  $y_i = \dot{q}_i + \lambda_i q_i$

Stability analysis is same, but satisfied the position synchronize.

### Simulation Result for Non-redundant manipulators

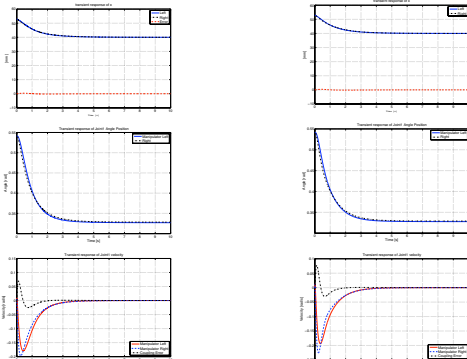
No information sharing      With information sharing



Simulation with different manipulator parameters and same initial states :  $M_L, I_L = 5M_L, 5I_L$ , Gain well tuned

### Simulation Result for Redundant manipulators

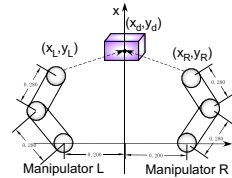
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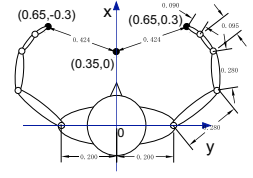
Simulation with different manipulator parameters and same initial states :  $M_L, I_L = 2M_L, 2I_L$ , Gain well tuned

### Simulation Setting

#### • Non-redundant



#### • Redundant



#### • Parameter

$L_1 = L_2 = 0.28$   
 $M_1 = 1.407, M_2 = 1.108$   
 $I_1 = 9.758 \times 10^{-3}$   
 $I_2 = 7.73 \times 10^{-3}$

#### • Parameter

$L_1 = L_2 = 0.28$ ,  
 $L_3 = 0.095, L_4 = 0.09$   
 $M_1 = 1.407, M_2 = 1.078$ ,  
 $M_3 = 0.242, M_4 = 0.0255$   
 $I_1 = 9.758 \times 10^{-3}$   
 $I_2 = 7.73 \times 10^{-3}$   
 $I_3 = 2.004 \times 10^{-4}$   
 $I_4 = 1.78 \times 10^{-5}$

### Simulation Result for Redundant manipulators

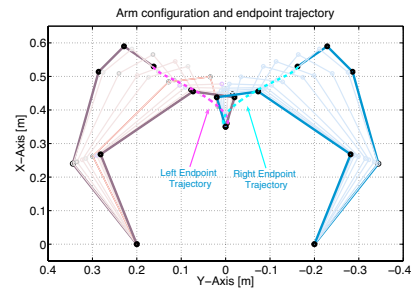


Figure: Trajectory of the robot manipulator and end-point

Simulation with the same parameter and initial states

### Conclusion of the simulation result

- Each situation of the simulations
  - End-point stable to reach the target point
  - Joint velocity stable to asymptotically
- With the same parameter and initial states
  - Off cause have the same reaching motion
- Different parameter or initial states or both
  - When bad tuning  $\Rightarrow$  Good advantage with cooperative but bad calculate performance
  - When well tuning  $\Rightarrow$  small advantage with cooperative but good calculate performance

## Conclusion and future works

### In this seminar

- Proposal of the "Cooperative reaching control"
  - Two parts of the controller "Reaching Control" and "Cooperative control"
- Stability and the proof

### Current and Future Works

- Consider the EXOS method
- Visual feedback to estimate the end-point position
- Experiment