

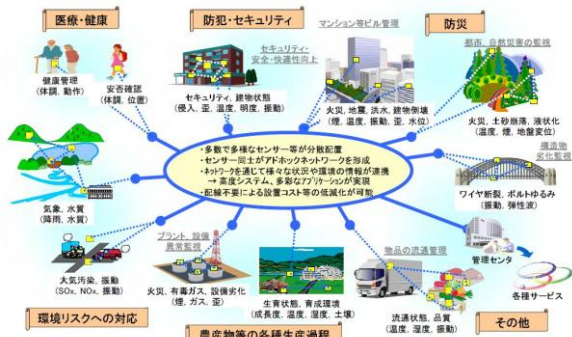
# Introduction to Sensor Networks



FL07-18-1  
Tatsuya Miyano



## Introduction



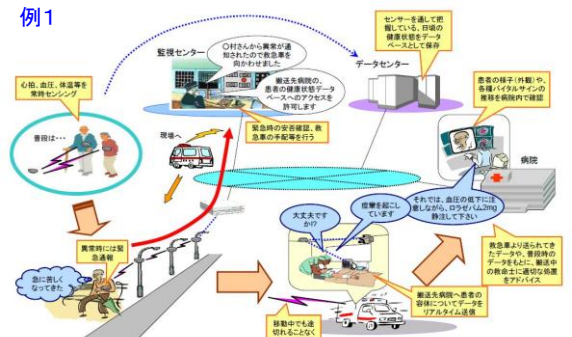
総務省 ユビキタスセンサネットワーク技術に関する調査研究会報告書(平成16年7月)

## Outline

1. Introduction
2. Mobile Ad Hoc Networks
3. Controlled Mobility
4. Sensor Coverage
5. Network-Based Control
6. Conclusions and Future Works



## Introduction



総務省 ユビキタスセンサネットワーク技術に関する調査研究会報告書(平成16年7月)



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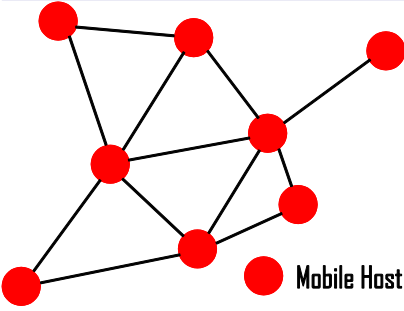
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## Mobile Ad Hoc Networks

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Mobile Ad Hoc Networks:  
The Wireless Networks constructed by only **Mobile Hosts**.



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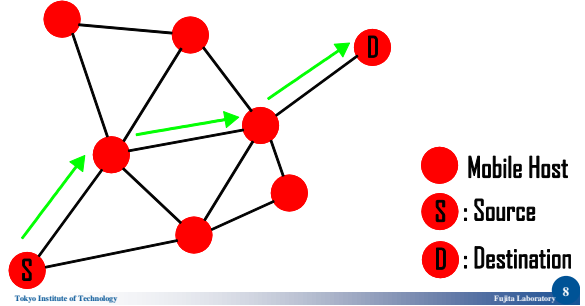
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## Routing

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Routing: Selecting the optimal route from the source to the destination.



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## Routing

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Routing **with** Location Information

I. Stojmenovic, 2002.

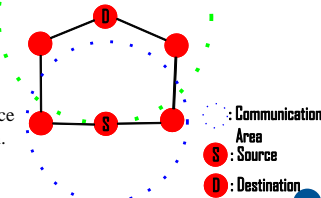
### Greedy Routing

A node selects neighboring node that is **closest to the destination** among its neighbors.

**Local Minimum**



A node sometimes **fails** to advance a message toward the destination.



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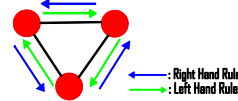
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## Routing

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### Face Routing



Route from S to D:

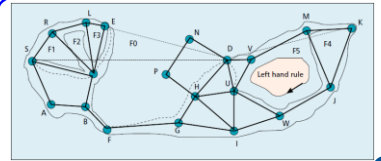
SCRCLERSABFGIWKMDV

### Greedy-Face-Greedy Routing

Greedy Routing  $\longleftrightarrow$  Face Routing

**Switch**

Route from S to D:  
SCE-ECBF-FGHD



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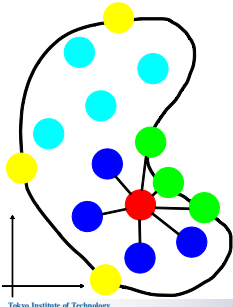


## Routing

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Routing **without** Location Information

A. Jadbabaie, 2004.



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## Routing

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$$\begin{bmatrix} \mathbf{x}_i(\mathbf{k}+1) \\ \mathbf{y}_i(\mathbf{k}+1) \end{bmatrix} = \begin{bmatrix} \mathbf{x}_i(\mathbf{k}) \\ \mathbf{y}_i(\mathbf{k}) \end{bmatrix} \quad i = 1, 2, \dots, m$$

$$\begin{bmatrix} \mathbf{x}_i(\mathbf{k}+1) \\ \mathbf{y}_i(\mathbf{k}+1) \end{bmatrix} = \begin{bmatrix} \sum_{j \in \mathcal{N}_i} \alpha_j \mathbf{x}_j(\mathbf{k}) \\ \sum_{j \in \mathcal{N}_i} \alpha_j \mathbf{y}_j(\mathbf{k}) \end{bmatrix} \quad i = m+1, m+2, \dots, n$$

$\mathcal{N}_i$ : The Set of Neighbors of the  $i$ th Node  $d_i$ : Cardinality of that Set  
 $(\mathbf{x}_i(\mathbf{k}), \mathbf{y}_i(\mathbf{k}))$ : Coordinate of the  $i$ th Node at the time  $k$

The first  $m$  nodes are **at the boundary** and have **fixed known** coordinates.  
The remaining  $n - m$  nodes are **in the interior of the region** whose virtual coordinates **change** in accordance of the above iteration.

The above equation is written as

$$\mathbf{x}_{i \in \mathcal{I}}(\mathbf{k}+1) = (D+B)^{-1} A \mathbf{x}_{i \in \mathcal{I}}(\mathbf{k}) + (D+B)^{-1} [b_1 b_2 \dots b_m] \mathbf{x}_p$$

$$\mathbf{y}_{i \in \mathcal{I}}(\mathbf{k}+1) = (D+B)^{-1} A \mathbf{y}_{i \in \mathcal{I}}(\mathbf{k}) + (D+B)^{-1} [b_1 b_2 \dots b_m] \mathbf{y}_p$$

where  $\mathbf{x} = [\mathbf{x}_p, \mathbf{x}_{i \in \mathcal{I}}]^T$ .

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Theorem

In steady state, the virtual coordinates converge to points in the convex hull of the boundary nodes. Moreover, the coefficients of the virtual coordinates can be explicitly calculated as

$$\bar{\mathbf{x}} = \lim_{k \rightarrow \infty} \mathbf{x}_{i_{mk}}(\mathbf{k}) = (\mathbf{D} + \mathbf{B} - \mathbf{A})^{-1} [\mathbf{b}_1, \mathbf{b}_2, \dots, \mathbf{b}_m] \mathbf{x}_p$$

$$\bar{\mathbf{y}} = \lim_{k \rightarrow \infty} \mathbf{y}_{i_{mk}}(\mathbf{k}) = (\mathbf{D} + \mathbf{B} - \mathbf{A})^{-1} [\mathbf{b}_1, \mathbf{b}_2, \dots, \mathbf{b}_m] \mathbf{y}_p.$$

The key facts to prove the above theorem are as follows.

- $\rho((\mathbf{D} + \mathbf{B})^{-1} \mathbf{A}) < 1$
- $\sum_{i=0}^{\infty} [(\mathbf{D} + \mathbf{B})^{-1} \mathbf{A}]^i (\mathbf{D} + \mathbf{B})^{-1} = (\mathbf{D} + \mathbf{B} - \mathbf{A})^{-1}$



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Objectives

- Power Efficiency  
*e.g.* Cost of Transmission, Cost of Mobility.
- Robustness of Communications  
*e.g.* Network Size, Irregular Paths.

The proposed algorithms guarantee these properties.

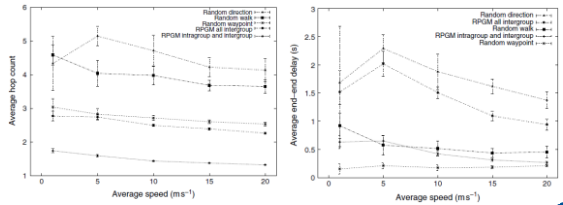
- Connectivity
- Convergence



Mobility Models for Ad Hoc Networks

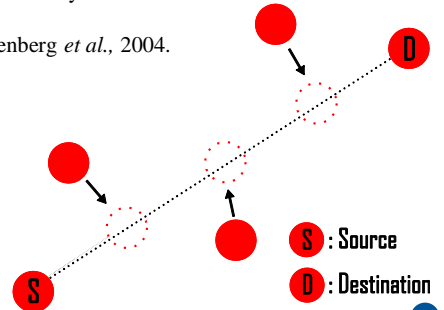
T. Camp *et al.*, 2002.

The performance of a routing protocol can vary significantly with different mobility models.



Mobility Control to Reach Optimality: the Synchronous or Asynchronous Scheme

David K. Goldenberg *et al.*, 2004.



Synchronous Mobility-Control Algorithm

- ▶  $\mathbf{x}_i$  : current position of node  $i$ .
  - ▶  $\mathbf{x}_{i-1}$  and  $\mathbf{x}_{i+1}$  : positions of nodes  $i - 1$  and  $i + 1$ .
  - ▶  $\mathbf{x}'_i$  : updated position of node  $i$ .
  - ▶  $g \in (0, 1]$  : damping factor.
  - ▶  $L$  and  $R$  : internal boolean state variables.
  - ▶ *moving* <sub>$i$</sub>  : message signaling node  $i$  starting to move.
- repeat**
- send  $\mathbf{x}_i$  to neighbors  $i - 1$  and  $i + 1$
  - receive  $\mathbf{x}_{i-1}$  and  $\mathbf{x}_{i+1}$
  - move toward  $\mathbf{x}'_i = \mathbf{x}_i + g \left[ \frac{\mathbf{x}_{i-1} + \mathbf{x}_{i+1}}{2} - \mathbf{x}_i \right]$
- until** (convergence)



Asynchronous Mobility-Control Algorithm

```

repeat
  send  $\mathbf{x}_i$  to neighbors  $i - 1$  and  $i + 1$ 
  repeat listen() until ( $L \wedge R == True$ )
  send  $\mathbf{moving}_i$  to neighbors  $i - 1$  and  $i + 1$ 
  set  $L := False, R := False$ 
  move toward  $\mathbf{x}'_i = \mathbf{x}_i + \mathbf{g} \left[ \frac{x_{i-1} + x_{i+1}}{2} - x_i \right]$ 
  repeat listen() until (arrive in bounded delay)
until (convergence)
subroutine listen():
  upon receive  $\mathbf{x}_{i-1}$  do  $L := True$ 
  upon receive  $\mathbf{x}_{i+1}$  do  $R := True$ 
  upon receive  $\mathbf{moving}_i$  do  $L := False$ 
  upon receive  $\mathbf{moving}_i$  do  $R := False$ 

```

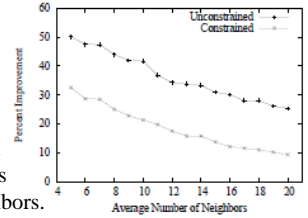


Simulation Results of Power Efficiency

Cost of Transmission:  $P(\mathbf{d}) = a + b d^\alpha$   
 Cost of Mobility:  $P_m(\mathbf{d}) = k d$   
 $a, b, k$ : Constant  $\alpha \in [2, 6]$   $d$ : Distance

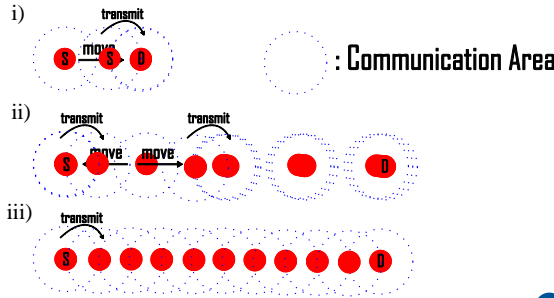
e.g.  
 $a = 10^{-7}$   $b = 10^{-9}$   
 $\alpha = 3$   $k = 0.1$

The constraint is that a communicating node does not move beyond the maximum communication range away from any of its non-communicating neighbors.



WISER/s

R. Suzuki et al., 2006.



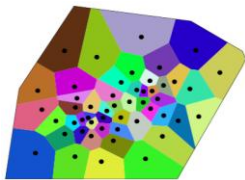
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Voronoi Partition

Given  $S \subset \mathbb{R}^2$  and a set  $\mathcal{P} = \{\mathbf{p}_1, \mathbf{p}_2, \dots, \mathbf{p}_n\} \subset S$  of  $n$  distinct points, the Voronoi partition of  $S$  generated by  $\mathcal{P}$  is the collection of sets  $\{V_1(\mathcal{P}), V_2(\mathcal{P}), \dots, V_n(\mathcal{P})\}$  defined by

$$V_i(\mathcal{P}) = \{q \in S \mid \|q - \mathbf{p}_i\| \leq \|q - \mathbf{p}_j\|, \forall \mathbf{p}_j \in \mathcal{P}\}.$$



S. Martinez et al., 2007.



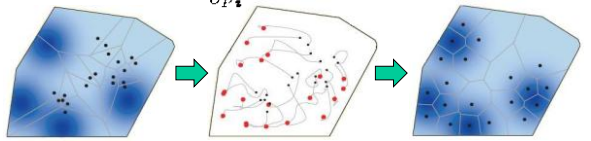
Distortion Problem

$f(\|q - \mathbf{p}_i\|)$ : Performance Function  $\phi(q)$ : Density Function

$H(\mathcal{P})$ : Distortion Function

$$H(\mathcal{P}) = \sum_{i=1}^n \int_{V_i(\mathcal{P})} f(\|q - \mathbf{p}_i\|) \phi(q) dq$$

$$\mathbf{u}_i = -\frac{\partial H}{\partial \mathbf{p}_i}$$



S. Martinez et al., 2007.



## Sensor Coverage

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Mobile Sensor Network Deployment using Potential Fields

$U$ : Scalar Potential Field  $F$ : Force  $\mathbf{x}$ : Position of the Node  
 $\mathbf{x}_i$ : Position of the other Node or Obstacle  $\mathbf{r}_i = |\mathbf{x}_i - \mathbf{x}|$   
 $k$ : Coefficient  $m$ : Mass  $\nu$ : Viscosity Coefficient

$$U = k \sum_i \frac{1}{r_i} \quad F = -\nabla U \quad m\ddot{\mathbf{x}} + \nu\dot{\mathbf{x}} = F$$



A. Howard *et al.*, 2002.

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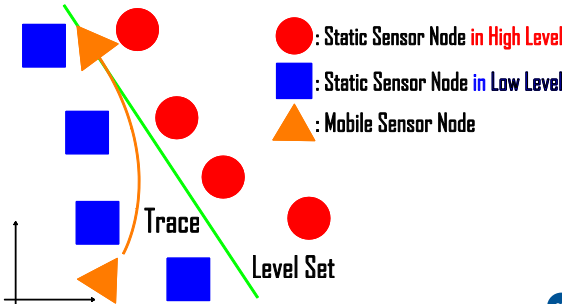


## Network-Based Control

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Level Set of Scalar Field

K. Dantu and G. S. Sukhatme, 2007.



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## Network-Based Control

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### Control Law

$$\dot{\mathbf{x}} = \alpha \text{Null}(\nabla G(\mathbf{x})) + \beta \nabla G(\mathbf{x})^\dagger$$

$$\nabla G(\mathbf{x}) = \nabla d_1(\mathbf{x}) - \nabla d_2(\mathbf{x})$$

$G(\mathbf{x})$  = (sensor reading at the mobile node) –  
(threshold reading defining the contour to be traced)

$\alpha, \beta$ : Scalar Gains  $\text{Null}(\nabla G(\mathbf{x}))$ : Null Space of  $\nabla G(\mathbf{x})$   
 $\nabla G(\mathbf{x})^\dagger$ : Penrose Pseudoinverse of  $\nabla G(\mathbf{x})$   
 $\nabla d_1(\mathbf{x})$ : Direction of the Node with the Highest Gain Increase Ratio.  
 $\nabla d_2(\mathbf{x})$ : Direction of the Node with the Highest Gain Decrease Ratio.

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## Network-Based Control

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### Algorithm for the Mobile Sensor Node

```

loop
  for  $i \in \{\text{Current neighbor list of mobile node}\}$  do
     $loc[i] \leftarrow$  Location of  $i$ 
     $sense[i] \leftarrow$  Sensor reading of  $i$ 
  end for
   $n1 \leftarrow$  Node with best gain increase gradient {using  $loc[]$  and  $sense[]$ }
   $n2 \leftarrow$  Node with best gain decrease gradient {using  $loc[]$  and  $sense[]$ }
  Compute  $\nabla d_1(\mathbf{x})$  and  $\nabla d_2(\mathbf{x})$ 
  Compute  $\nabla G(\mathbf{x})$  and  $G(\mathbf{x})$ 
  Compute  $\dot{\mathbf{x}}$ 
  Command  $\dot{\mathbf{x}}$  to actuators
end loop

```

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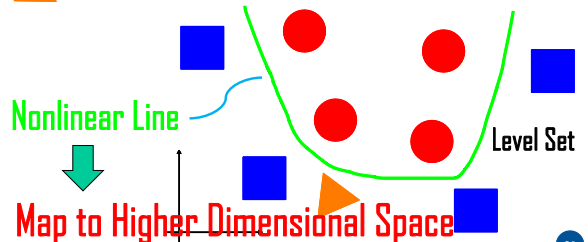
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## Network-Based Control

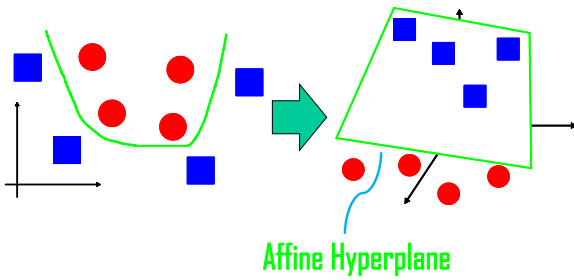
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- : Static Sensor Node in High Level
- : Static Sensor Node in Low Level
- ▲: Mobile Sensor Node



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### Conclusions

I surveyed Sensor Networks.

### Future Works

- Controlled Mobility
  - Balancing the Power Usage of each Node.
- Network-Based Control
  - Specifying the Problem.
  - Studying Support Vector Machine.